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SI-MATH1T

| Part A: Introduction        |                                |   |                        |
|-----------------------------|--------------------------------|---|------------------------|
| Program: Certificate Course |                                | Class: B.Sc. I Year   | Year: 2021             |
|                             |                                | Session: 2021-2022  |                        |
| Subject: Mathematics        |                                |   |                        |
| 1                           | Course Code                    | SI-MATH1T   |                        |
| 2                           | Course Title                   | Algebra, Vector Analysis and Geometry (Paper 1)   |                        |
| 3                           | Course Type                    | Core Course   |                        |
| 4                           | Pre-requisite (if any)         | To study this course, a student must have had the subject Mathematics in class 12 <sup>th</sup> .   |                        |
| 5                           | Course Learning Outcomes (CLO) | The course will enable the students to: <ol style="list-style-type: none"> <li>1. Recognize consistent and inconsistent systems of linear equations by the row echelon form of the augmented matrix, using the rank of matrix.</li> <li>2. To find the Eigen values and corresponding Eigen vectors for a square matrix.</li> <li>3. Using the knowledge of vector calculus in geometry.</li> <li>4. Enhance the knowledge of three dimensional geometrical figures (eg. cone and cylinder).</li> </ol> |                        |
| 6                           | Credit Value                   | Theory: 6   |                        |
| 7                           | Total Marks                    | Max. Marks: 25 + 75   | Min. Passing Marks: 33 |

| Part B: Content of the Course                               |   |                 |
|---|---|-----------------|
| Total No. of Lectures (in hours per week): 3 hours per week |   |                 |
| Total Lectures: 90 hours                                    |   |                 |
| Unit  | Topics  | No. of Lectures |
| I   | 1.1 Historical background: <ul style="list-style-type: none"> <li>1.1.1 Development of Indian Mathematics: Later Classical Period (500 -1250)</li> <li>1.1.2 A brief biography of Varahamihira and Aryabhata</li> </ul> 1.2 Rank of a Matrix<br>1.3 Echelon and Normal form of a matrix<br>1.4 Characteristic equations of a matrix <ul style="list-style-type: none"> <li>1.4.1 Eigen-values</li> <li>1.4.2 Eigen-vectors</li> </ul> | 15              |
| II  | 2.1 Cayley Hamilton theorem<br>2.2 Application of Cayley Hamilton theorem to find the inverse of a matrix.<br>2.3 Application of matrix to solve a system of linear equations<br>2.4 Theorems on consistency and inconsistency of a system of linear equations<br>2.5 Solving linear equations up to three unknowns   | 18              |

Report —  
(Dr Anil Rajput)



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| III  | 3.1 Scalar and Vector products of three and four vectors<br>3.2 Reciprocal vectors<br>3.3 Vector differentiation<br>3.3.1 Rules of differentiation<br>3.3.2 Derivatives of Triple Products<br>3.4 Gradient, Divergence and Curl<br>3.5 Directional derivatives<br>3.6 Vector Identities<br>3.7 Vector Equations   | 18 |
| IV   | 4.1 Vector Integration<br>4.2 Gauss theorem (without proof) and problems based on it<br>4.3 Green theorem (without proof) and problems based on it<br>4.4 Stoke theorem (without proof) and problems based on it  | 15 |
| V  | 5.1 General equation of second degree<br>5.2 Tracing of conics<br>5.3 System of conics<br>5.4 Cone<br>5.4.1 Equation of cone with given base<br>5.4.2 Generators of cone<br>5.4.3 Condition for three mutually perpendicular generators<br>5.4.4 Right circular cone<br>5.5 Cylinder<br>5.5.1 Equation of cylinder and its properties<br>5.5.2 Right Circular Cylinder<br>5.5.3 Enveloping Cylinder | 24 |
| <b>Keywords:</b><br>Indian Mathematics, Rank of a Matrix, Scalar and Vector products, Vector differentiation, Vector identities, Vector integration, General equation of second degree, Tracing of conics, System of conics, Equation of cone, Equation of cylinder. |   |    |

### Part C - Learning Resources

Text Books, Reference Books, Other Resources

#### Suggested Readings:

##### Text Books:

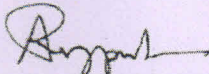
1. K. B. Datta: Matrix and Linear Algebra, Prentice Hall of India Pvt. Ltd. New Delhi 2000.
2. Shanti Narayan: A Text Book of Vector Calculus, S. Chand & Co., New Delhi, 1987.
3. S. L. Loney: The Elements of Coordinate Geometry Part-1, New Age International (P) Ltd., Publishers, New Delhi, 2016.
4. P. K. Jain and Khalil Ahmad: A text book of Analytical Geometry of Three Dimensions, Willey Eastern Ltd, 1999.
5. Gerard G. Emch, R. Sridharan, M. D. Srinivas: Contributions to the History of Indian Mathematics, Hindustan Book Agency, Vol. 3, 2005.

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| Part A: Introduction        |                                |  |                        |
|-----------------------------|--------------------------------|--|------------------------|
| Program: Certificate Course |                                | Class: B.Sc. 1 Year  | Year: 2021             |
|                             |                                | Session: 2021-2022   |                        |
| Subject: Mathematics        |                                |  |                        |
| 1                           | Course Code                    | SI-MATH2T  |                        |
| 2                           | Course Title                   | Calculus and Differential Equations (Paper 2)  |                        |
| 3                           | Course Type                    | Core Course  |                        |
| 4                           | Pre-requisite (if any)         | To study this course, a student must have had the subject Mathematics in class 12 <sup>th</sup> .  |                        |
| 5                           | Course Learning Outcomes (CLO) | <p>The course will enable the students to:</p> <ol style="list-style-type: none"> <li>1. Sketch curves in a plane using its Mathematical properties in the different coordinate systems of reference.</li> <li>2. Using the derivatives in Optimization, Social sciences, Physics and Life sciences etc.</li> <li>3. Formulate the Differential equations for various Mathematical models.</li> <li>4. Using techniques to solve and analyze various Mathematical models.</li> </ol> |                        |
| 6                           | Credit Value                   | Theory: 6  |                        |
| 7                           | Total Marks                    | Max. Marks: 25 + 75  | Min. Passing Marks: 33 |

| Part B: Content of the Course                               |  |                 |
|---|--|-----------------|
| Total No. of Lectures (in hours per week): 3 hours per week |  |                 |
| Total Lectures: 90 hours                                    |  |                 |
| Unit  | Topics   | No. of Lectures |
| 1   | 1.1 Historical background: <ul style="list-style-type: none"> <li>1.1.1 Development of Indian Mathematics: Ancient and Early Classical Period (till 500 CE)</li> <li>1.1.2 A brief biography of Bhāskaracharya (with special reference to Lilavati) and Madhava</li> </ul> 1.2 Successive differentiation <ul style="list-style-type: none"> <li>1.2.1 Leibnitz theorem</li> <li>1.2.2 Maclaurin's series expansion</li> <li>1.2.3 Taylor's series expansion</li> </ul> 1.3 Partial Differentiation <ul style="list-style-type: none"> <li>1.3.1 Partial derivatives of higher order</li> <li>1.3.2 Euler's theorem on homogeneous functions</li> </ul> 1.4 Asymptotes <ul style="list-style-type: none"> <li>1.4.1 Asymptotes of algebraic curves</li> <li>1.4.2 Condition for Existence of Asymptotes.</li> <li>1.4.3 Parallel Asymptotes</li> <li>1.4.4 Asymptotes of polar curves</li> </ul> | 18              |

  
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| II   | 2.1 Curvature<br>2.1.1 Formula for radius of Curvature<br>2.1.2 Curvature at origin<br>2.1.3 Centre of Curvature<br>2.2 Concavity and Convexity<br>2.2.1 Concavity and Convexity of curves<br>2.2.2 Point of Inflexion<br>2.2.3 Singular point<br>2.2.4 Multiple points<br>2.3 Tracing of curves<br>2.3.1 Curves represented by Cartesian equation<br>2.3.2 Curves represented by Polar equation   | 18 |
| III  | 3.1 Integration of transcendental functions<br>3.2 Introduction to Double and Triple Integral<br>3.3 Reduction formulae<br>3.4 Quadrature<br>3.4.1 For Cartesian coordinates<br>3.4.2 For Polar coordinates<br>3.5 Rectification<br>3.5.1 For Cartesian coordinates<br>3.5.2 For Polar coordinates   | 18 |
| IV   | 4.1 Linear differential equations<br>4.1.1 Linear equation<br>4.1.2 Equations reducible to the linear form<br>4.1.3 Change of variables<br>4.2 Exact differential equations<br>4.3 First order and higher degree differential equations<br>4.3.1 Equations solvable for x, y and p<br>4.3.2 Equations homogenous in x and y<br>4.3.3 Clairaut's equation<br>4.3.4 Singular solutions<br>4.3.5 Geometrical meaning of differential equations<br>4.3.6 Orthogonal trajectories | 18 |
| V  | 5.1 Linear differential equation with constant coefficients<br>5.2 Homogeneous linear ordinary differential equations<br>5.3 Linear differential equations of second order<br>5.4 Transformation of equations by changing the dependent/independent variable<br>5.5 Method of variation of parameters  | 18 |
| <b>Keywords/Tags:</b><br>Indian Mathematics, Successive differentiation, Partial Differentiation, Asymptotes, Curvature, Tracing of curves, Quadrature, Rectification, Linear differential equations, Method of variation of parameters. |  |    |

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